

# Task Planning with OMT: an Application to Production Logistics

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# What is this presentation about?



Planning problem



What is task planning in logistics?

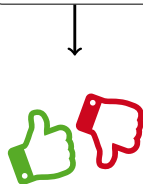
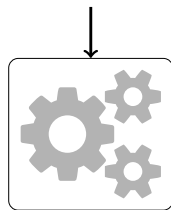


Plan



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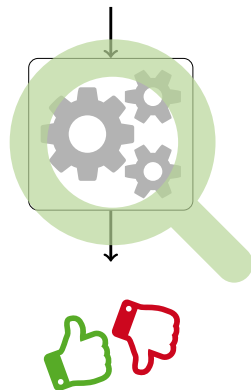
$$\neg \mathbf{a} \wedge \mathbf{b} \vee \mathbf{c}$$
$$\mathbf{x}^2 + \mathbf{x}_2 \quad \sqrt{\varphi}$$



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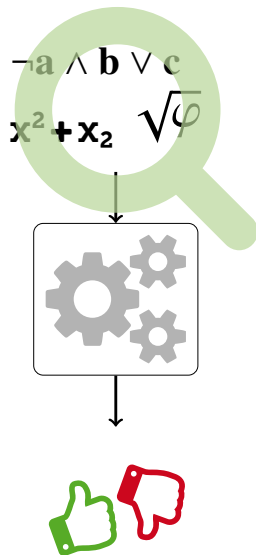
What is OMT?

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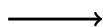
How can we use OMT for planning?



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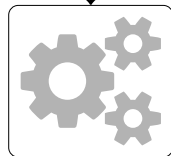


Planning problem



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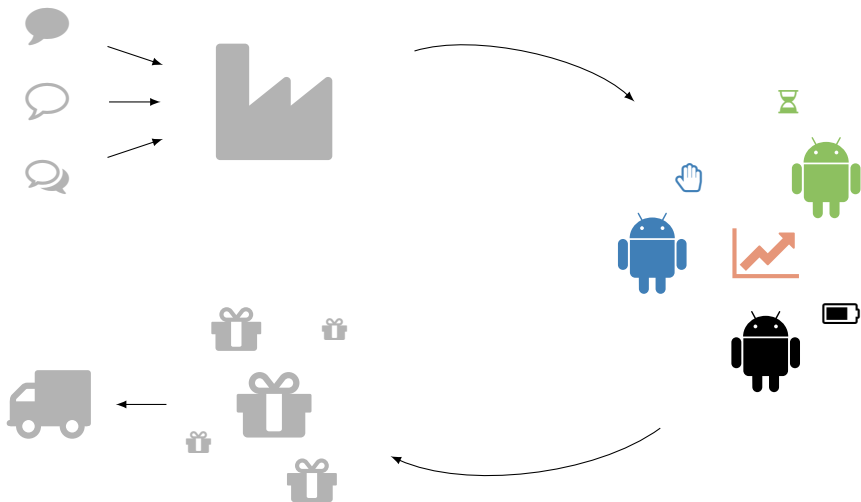
Plan

Can we use OMT for  
planning in logistics?

Before we go into the details. . .

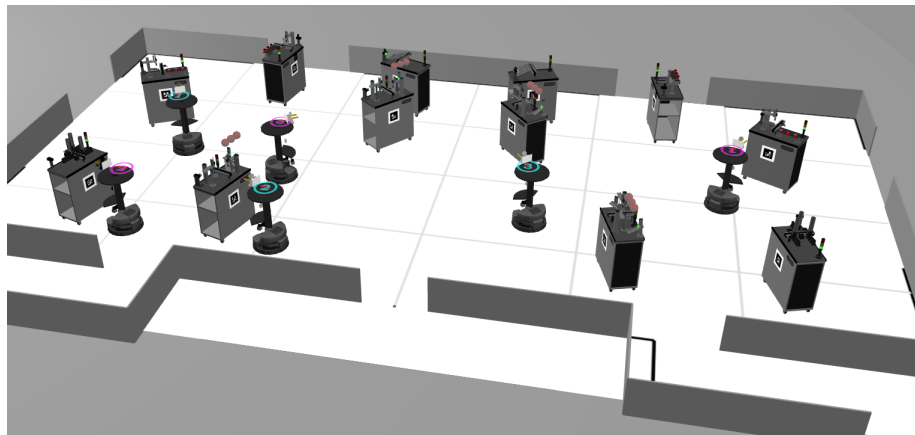
a little teaser

# Planning in the era of *Smart Factories*





# Planning & Execution Competition for Logistics Robots in Simulation



# Planning & Execution Competition for Logistics Robots in Simulation

Planning and execution for the RCLL. What's hard?

- time windows
- domain representation: over 250 configurations possible!
- combinatorics
- scalability
- execution on robots/machines that can break
- performance guarantees
- ...

# What is OMT?

$\varphi$

# Satisfiability Modulo Theories

Boolean abstraction

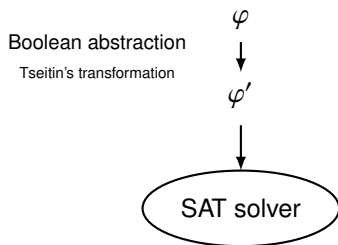
Tseitin's transformation

$\varphi$

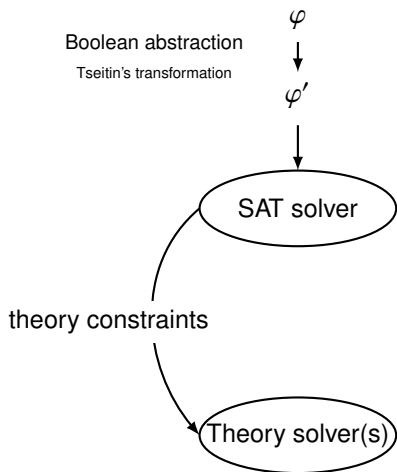


$\varphi'$

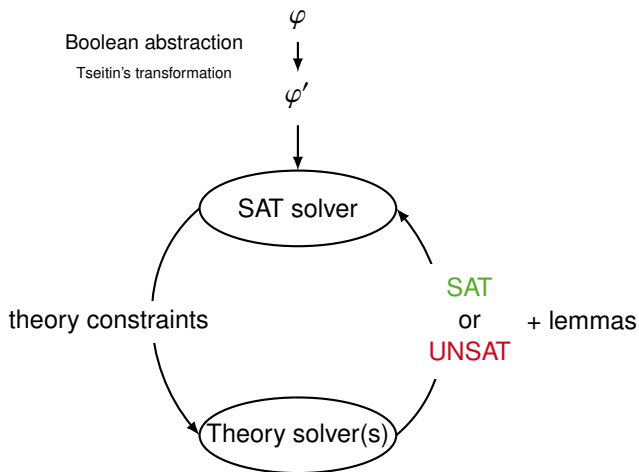
# Satisfiability Modulo Theories



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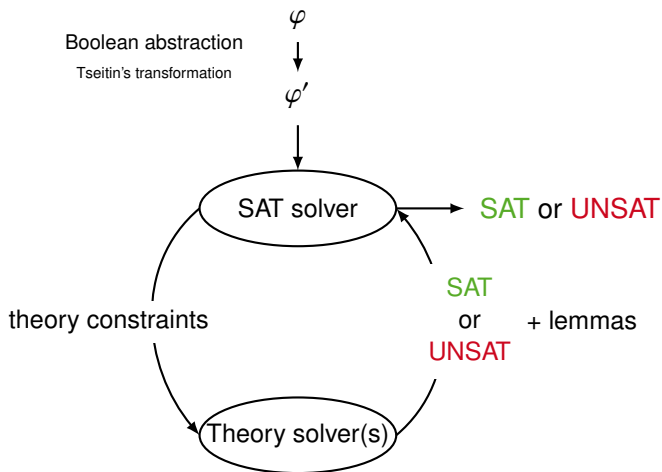


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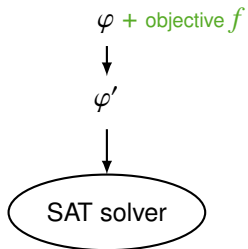


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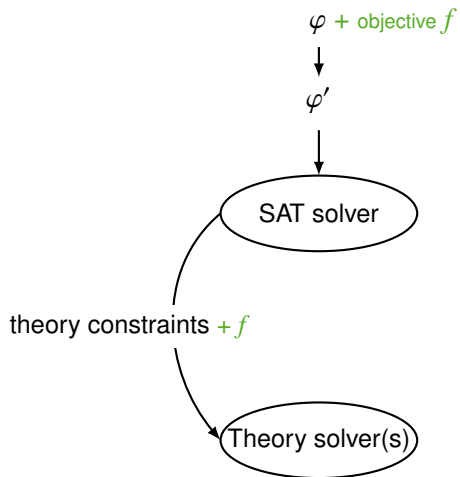


$\varphi$

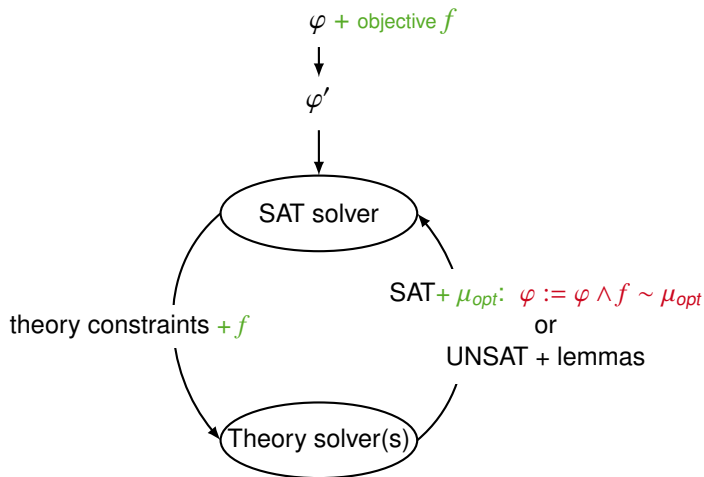
$\varphi$  + objective  $f$



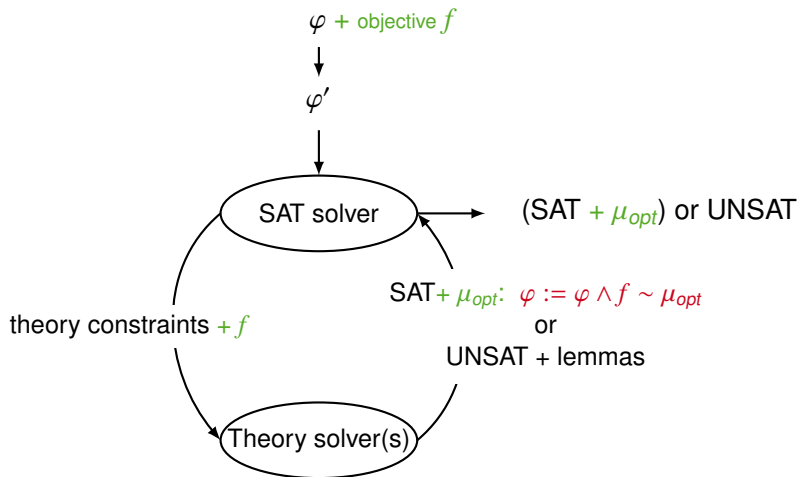
# Optimization Modulo Theories



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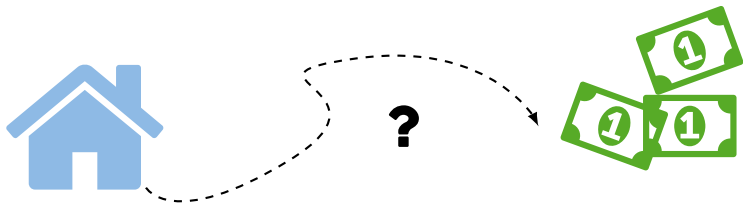
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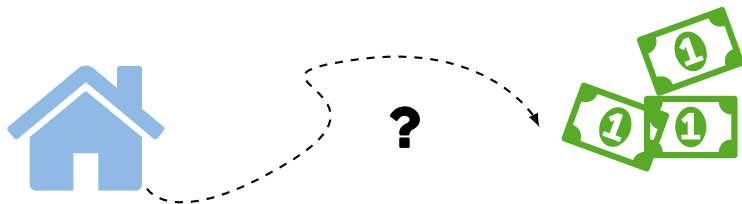
How can we use OMT for planning?



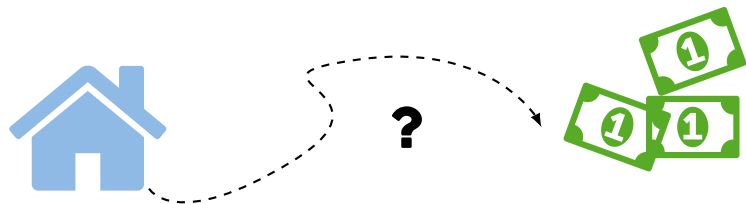
# Planning as Satisfiability



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💡 restrict search for a plan to paths with (predetermined) bound



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Reductions of planning to SAT

- linear encodings[Kautz and Selman, 1992]
- later extended, e.g., concurrency, theories...

# Planning as Satisfiability

## Planning problem

Let  $\mathcal{F}$  and  $\mathcal{A}$  be the sets of *fluents* and *actions*.

Let  $\mathcal{X} = \mathcal{F} \cup \mathcal{A}$  and  $\mathcal{X}' = \{x' : x \in \mathcal{X}\}$  be its *next state* copy.

A planning problem is a triple of boolean formulae  $\Pi = \langle I, T, G \rangle$  where

- $I(\mathcal{F})$  represents the set of *initial* states
- $T(\mathcal{X}, \mathcal{X}')$  describes how actions *affect* states
- $G(\mathcal{F})$  represents the set of *goal* states

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## Encoding $\Pi$ in SAT - the formula

The planning problem  $\Pi$  with makespan  $k$  is the formula

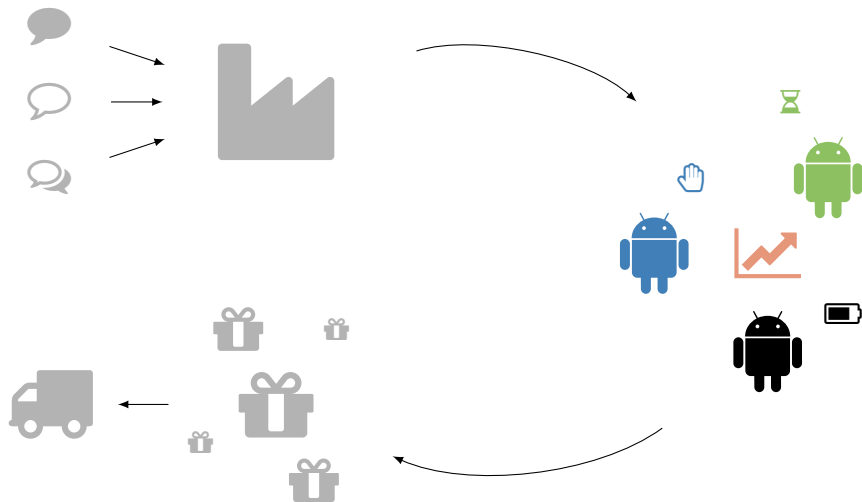
$$\varphi_{(\Pi, k)} := I(\mathcal{X}_0) \wedge \bigwedge_{i=0}^{k-1} T(\mathcal{X}_i, \mathcal{X}_{i+1}) \wedge G(\mathcal{X}_k)$$

## Encoding $\Pi$ in SAT

- $\varphi_{(\Pi,k)}$  is sat iff there exists a plan with length  $k$ 
  - ✓ in that case, a plan can be extracted from the satisfying assignment
- in parallel encodings, two actions can be executed in parallel if they are non-mutex
- optimal plans minimize the number of steps:
  - ▶ start with  $k = 1$
  - ↻ increase until  $\varphi_{(\Pi,k)}$  becomes sat or upper bound on  $k$  is reached.

Can we use OMT for planning in logistics?

# Planning in the era of *Smart Factories*





Planning in production logistics is tough!

Many factors must be considered while planning

- state space of possible configurations
- efficiency of production processes
- costs/rewards
- ...

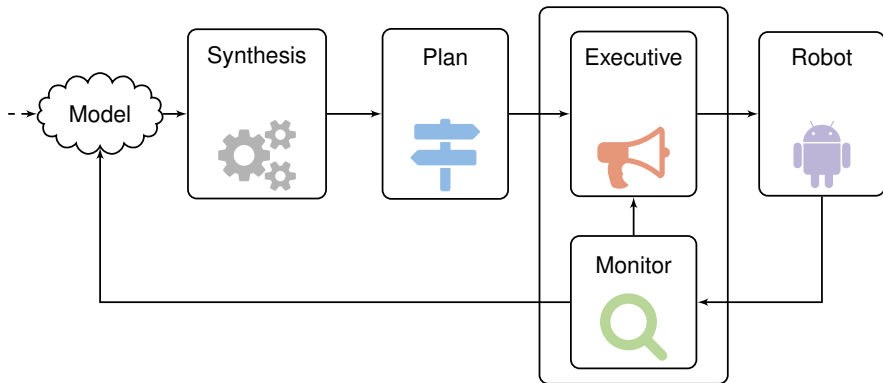
Trade-off: **fast heuristic** vs **optimal** solutions

## Objective



Study the feasibility of OMT planning in a non-trivial logistic domain

# Integrated synthesis and execution



1st place in the Planning and Execution Competition for Logistics Robots  
PExC @ ICAPS 2018

# Performance: a quick look

Planner	C0 – R1		C0 – R2		C0 – R3	
	Solved	Runtime (s)	Solved	Runtime (s)	Solved	Runtime (s)
<b>RCLLPlan -Sat</b>	<b>20</b>	0.98	<b>20</b>	2.52	<b>20</b>	2.73
<b>RCLLPlan -Opt</b>	<b>20</b>	15.22	17	42.18	4	54.26
POPF	<b>20</b>	20.73	4	25.66	0	-
Optic	13	24.39	2	57.60	0	-
SMTPlan+	0	-	0	-	0	-

## Achieved so far

- implemented a domain-specific planner for the RCLL
- planner is based on satisfiability checking and optimization
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Are we done?

There's still a lot to do to ease applicability of OMT technology in planning!



## Ongoing

Need a general approach for planning with OMT

- currently developing a domain-independent OMT planner
- use it as a platform to evaluate state of the art in SMT/OMT

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This is the starting point, several major challenges await:

- develop new reductions that are “solver friendly”
- exploit parallel solving, hybrid architectures
- how to explain decisions made by a solver?
- ... more in the paper ...



# More ideas?

